

# Virtual Formulation Laboratory for prediction and optimisation of manufacturability of advanced solids based formulations



Investigators: I.C. Sinka (PI), J.Y.Y. Heng, M. Ghadiri, M.S.A. Bradley, R.L. Davidchack, X. Jia,  
R. Berry (RIP), J. Cummins

PDRAs: B.D. Edmans, N. Di Pasquale, M. Pasha, H. Salehi, V. Karde, V. Garg (PhD student)

Future formulation 4  
University of Edinburgh (online meeting)  
23 June 2020

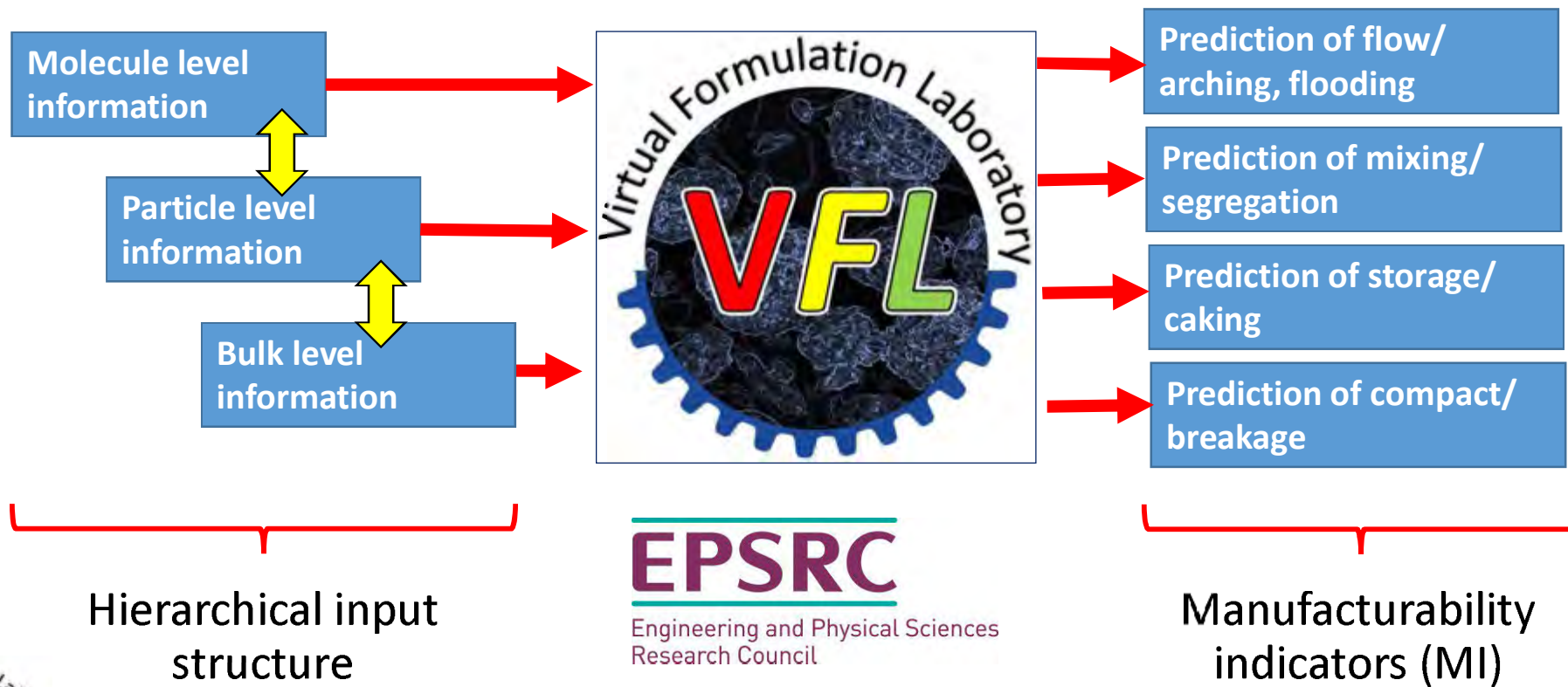


# Virtual Formulation Lab Team

Academic partners	PDRAs and visitors	Industrial partners
Prof. Csaba Sinka (PI) – Leicester Prof. Ruslan Davidchack	Dr. Ben Edmans Dr. Nicodemo Di Pasquale	CPI, NFC P&G GlaxoSmithKline AstraZeneca
Prof. Mojtaba Ghadiri – Leeds Dr. Xiaodong Jia	Dr. Mehrdad Pasha Dr. Koichiro Ogata (visiting scholar) Dr. Sadegh Nadimi (Leeds U.) Dr. Wenguang Nan (visiting scholar)	Nestle KP Snacks Brookfield Britest
Prof. Mike Bradley – Greenwich Dr. Rob Berry (RIP) John Cummins	Dr. Hamid Salehi Vivek Garg (PhD student) Dr. John Cummins (Greenwich U.)	PSE Griffiths Food Freeman Technology
Dr. Jerry Heng – Imperial College	Dr. Vikram Karde Izabela Phillips (PhD student)	Chemours EDEM Johnson Matthew Abbvie



# Virtual Formulation Laboratory for prediction and optimisation of manufacturability of advanced solids based formulations



# VFL work programmes

- Predicting bulk properties from particle properties
- Predicting particle properties from molecular structure
- Characterisation of adhesive interactions and surface energy of functionalised particles
- VFL toolkit development



# VFL approach to powder surface energy (I)

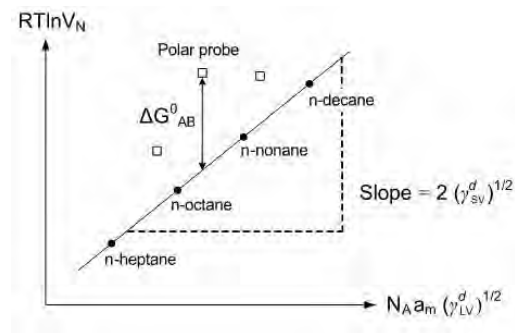
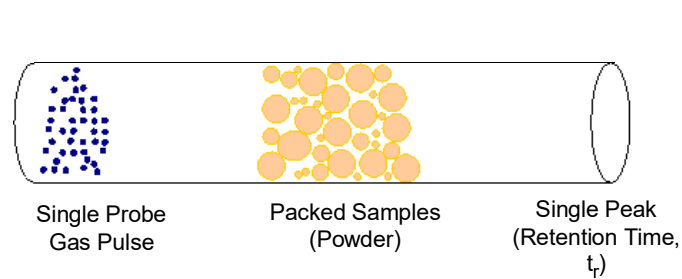
Vikram Karde and Jerry Heng

**Imperial College**  
London

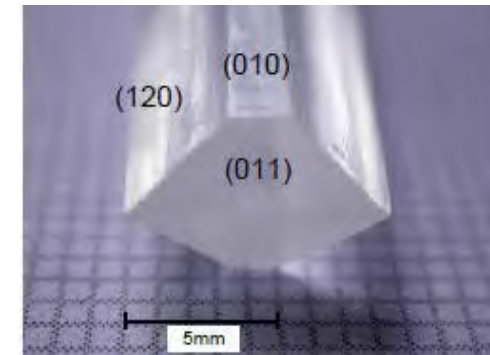


# Surface Energy Characterisation using Inverse Gas Chromatography (FD-IGC)

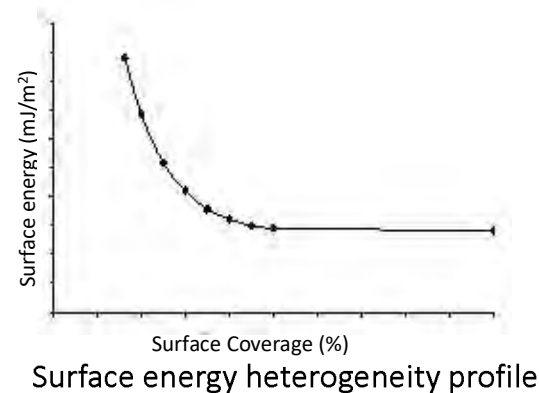
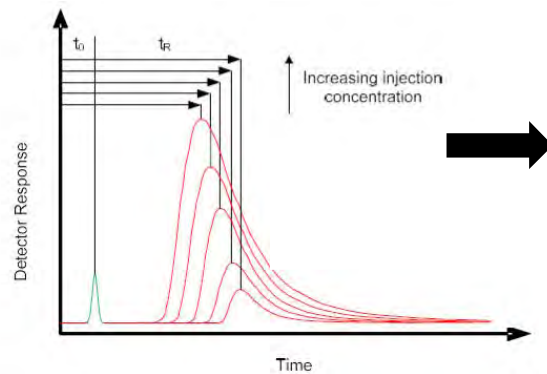
## Surface energy determination using IGC



## Anisotropy in crystalline solids (Heterogeneous surfaces)

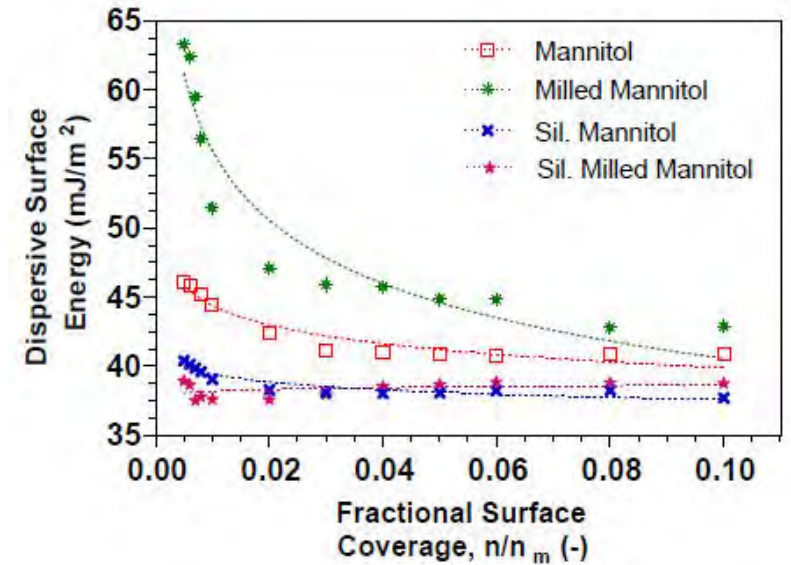
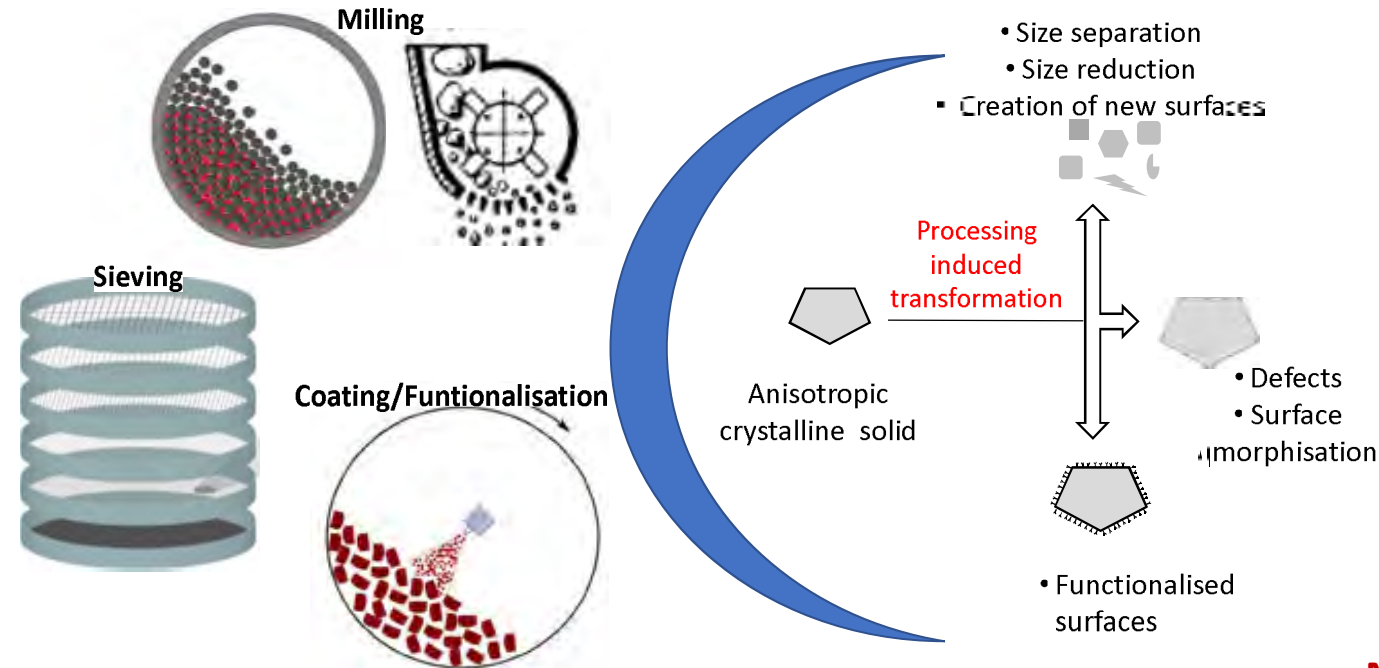


## Surface energy heterogeneity using Finite Dilution IGC (FD-IGC)



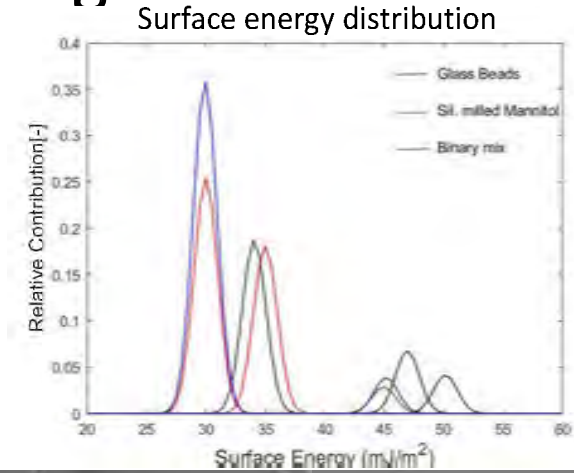
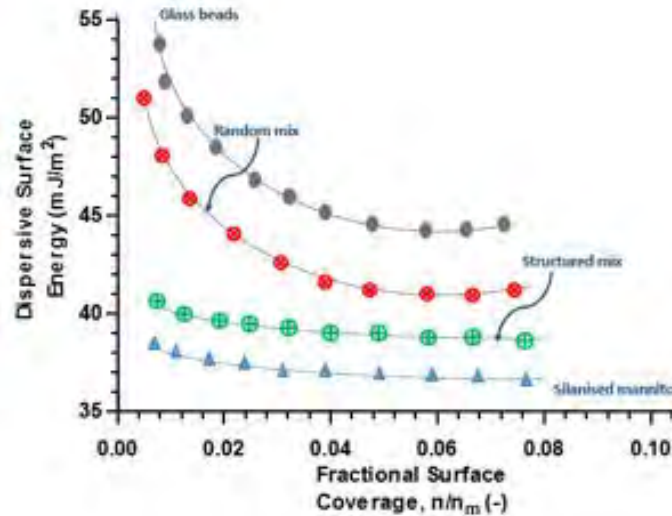
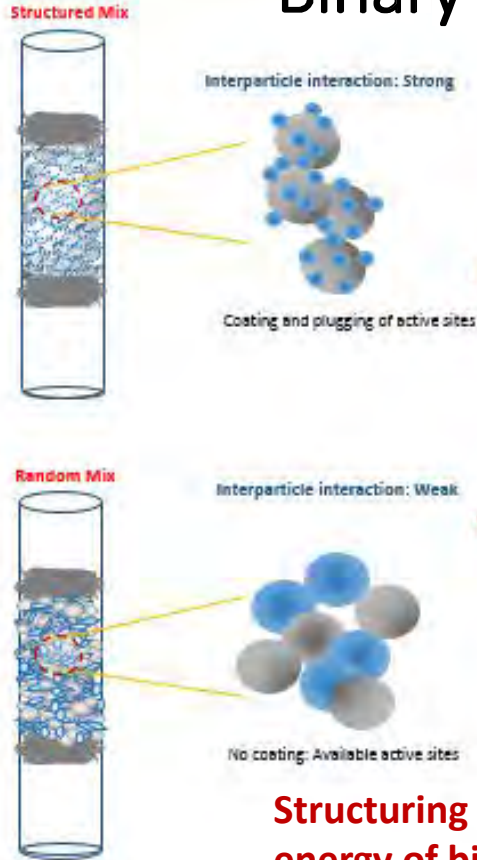
## Facet specific surface energy using Contact angle

# Processing and Surface Energy



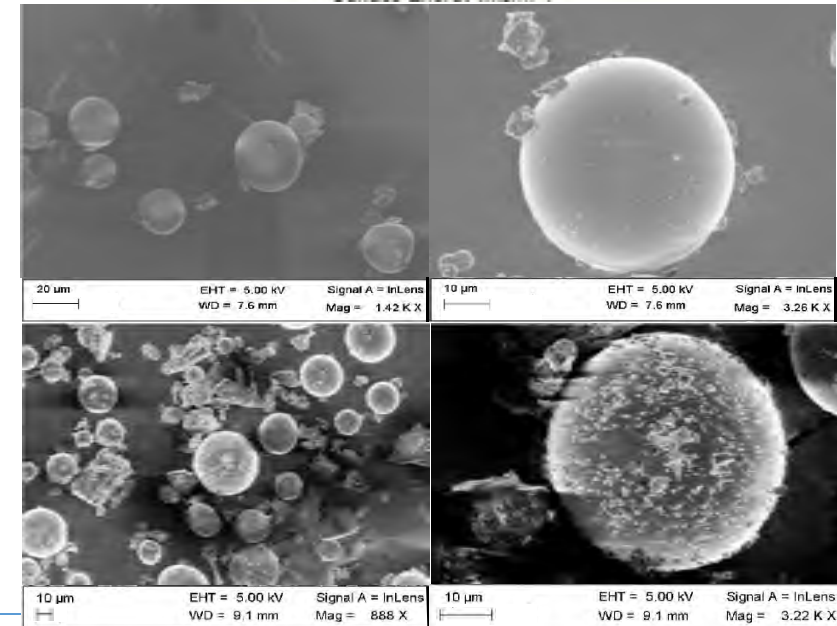
- **Milling induced surface damage led to high heterogeneity surface**
- **Functionalisation creates energetically homogeneous surfaces**

# Interparticle Structuring and Surface Energetics of Binary Mixtures



**Structuring of component particles influence the surface energy of binary mixture**

Karde et al.,(2020) Influence of interparticle structuring on the surface energetics of a binary powder system. *Int. J. Pharm.* **581**, 119295





# VFL approach to surface energy (II)

Nicodemo Di Pasquale and Ruslan Davidchack



## Shuttleworth Equation (1950)

Surface Stress tensor  $f_{ij}^{SS}$ , Surface Free Energy  $\gamma$ , strain tensor  $u_{ij}$

$$f_{ij}^{SE} \equiv \gamma \delta_{ij} + \frac{\partial \gamma}{\partial u_{ij}} = f_{ij}^{SS}, \quad i, j = x, y$$

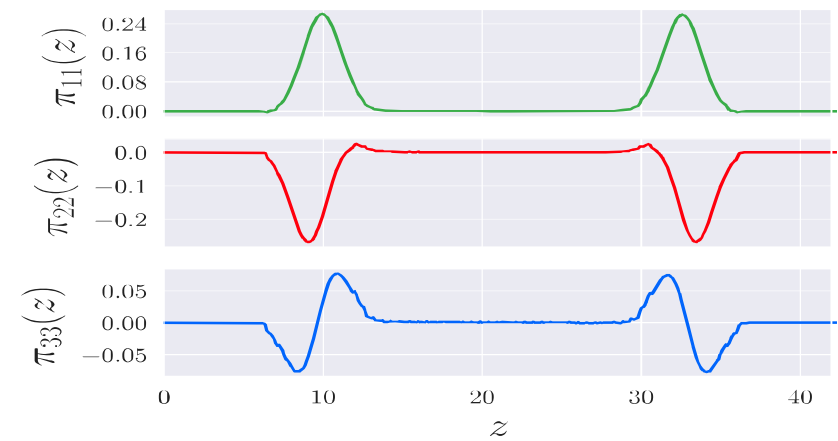
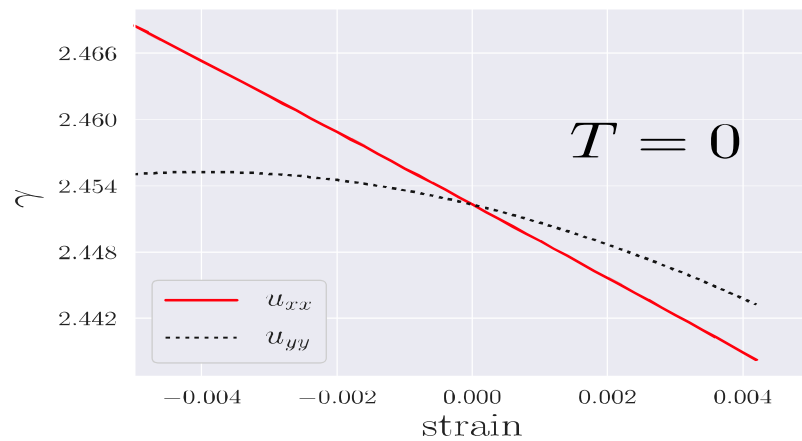
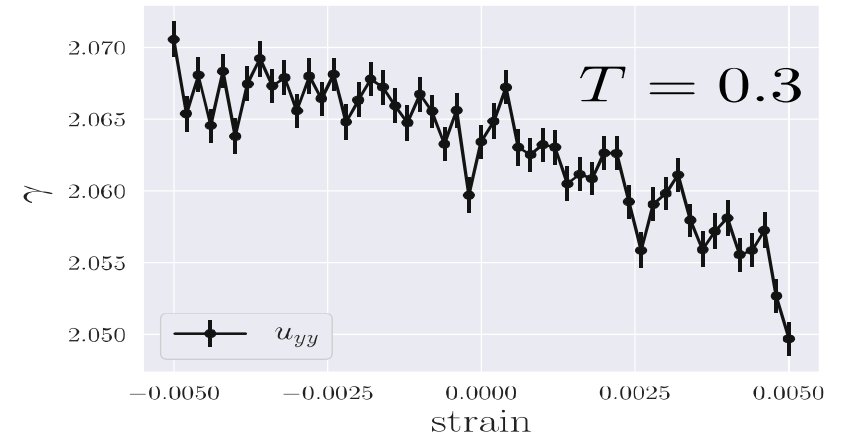
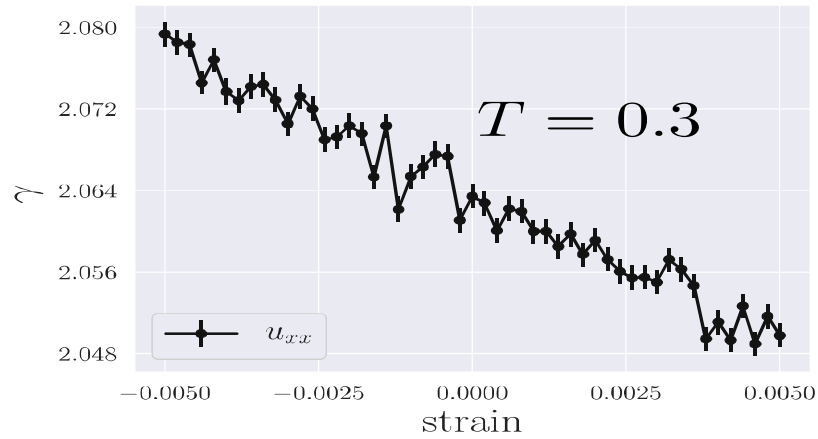
- $\frac{\partial \gamma}{\partial u_{ij}}$  can be positive or negative
- $\gamma$  always positive
- $f_{ij}$  can be positive or negative

## Verification for LJ crystal at finite temperature with cleaving

$T = 0.3$	$\gamma$	$\frac{\partial \gamma}{\partial u_{ij}}$	$f_{ii}^{SS}$	$f_{ii}^{SE}$
$u_{xx}$	2.063(2)	-2.87(6)	-0.783(8)	-0.81(6)
$u_{yy}$	2.063(2)	-1.38(6)	0.69(2)	0.68(6)

(Reduced LJ units, fcc(110))

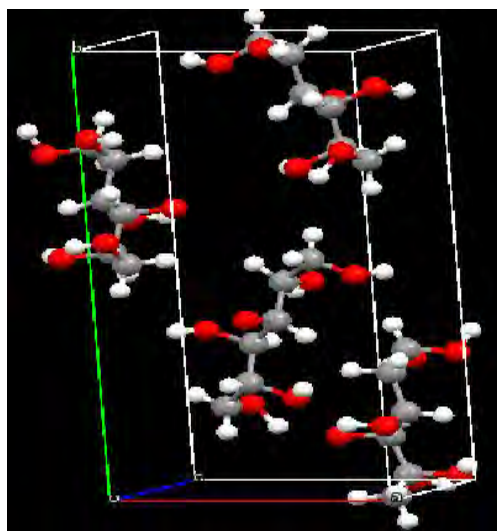
# LJ system: fcc(110)



Results in reduced LJ units

# Surface Free Energy organic crystals: Mannitol

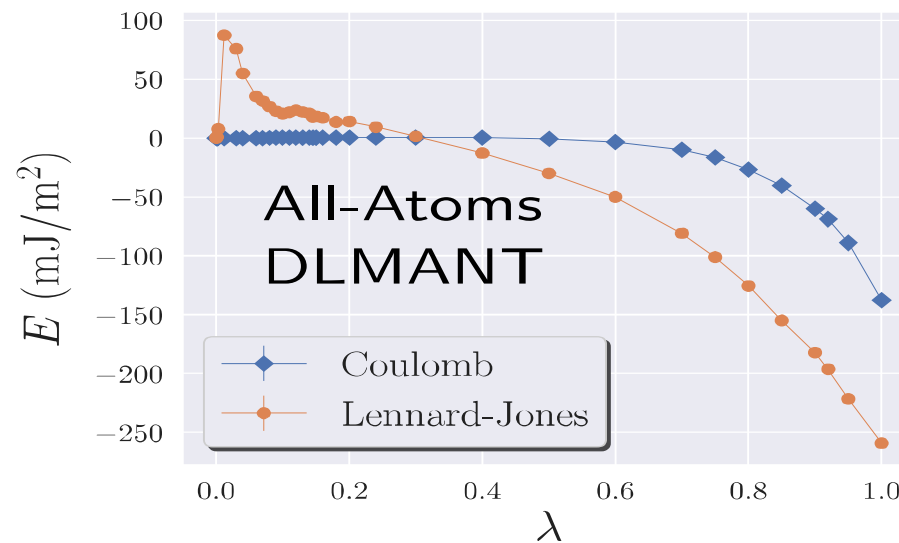
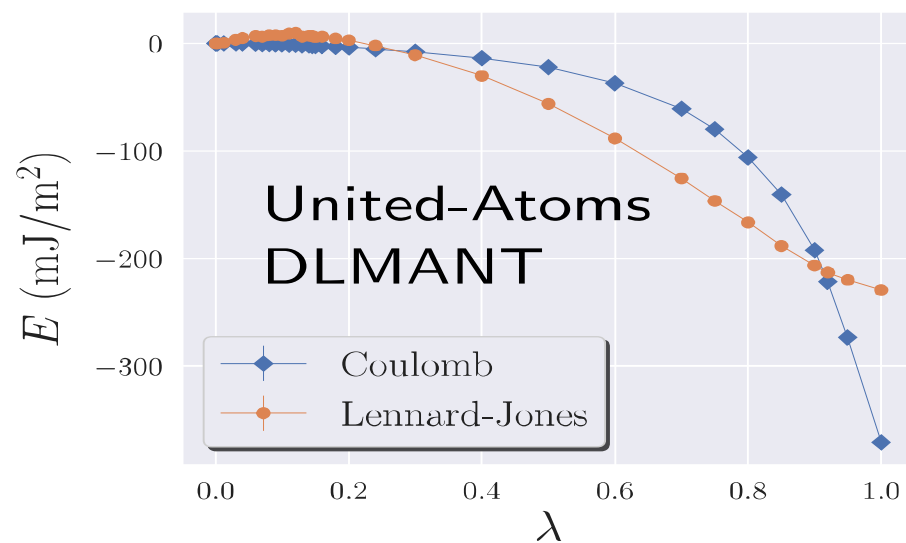
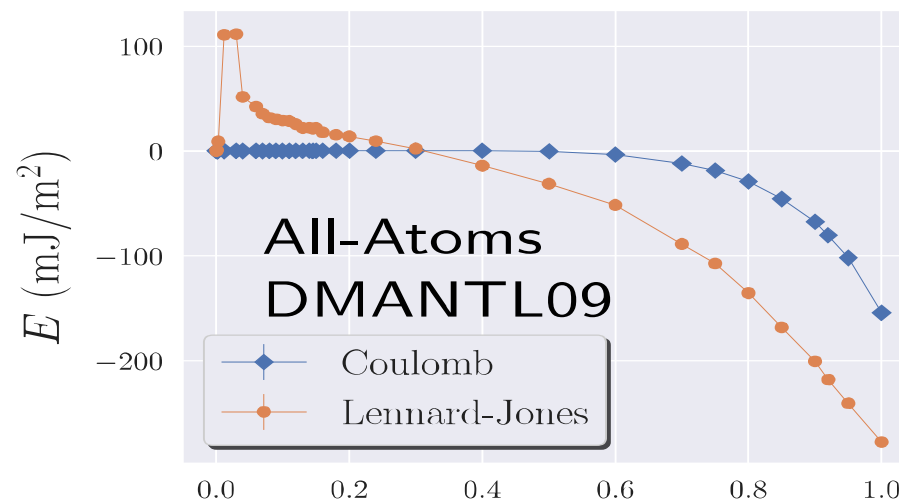
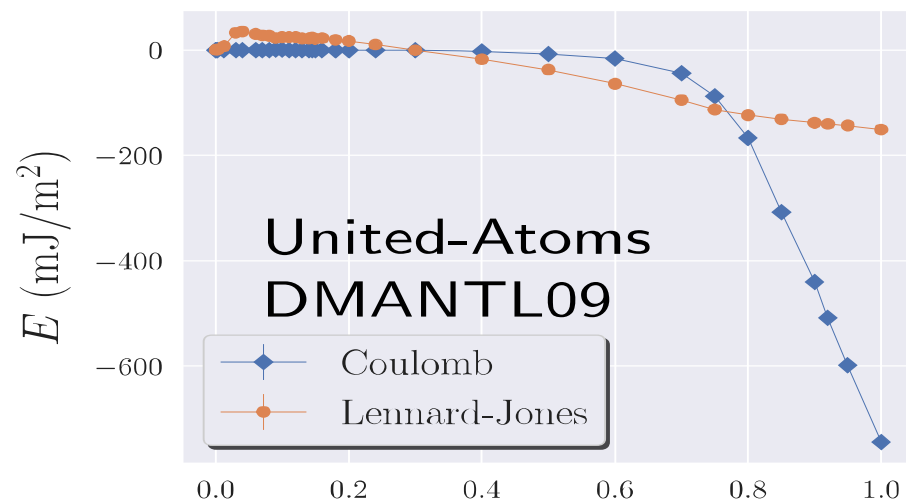
The cleaving methodology is applied to molecular crystals



- Different orientations considered: (001), (010), (100), (011), (120)
- Different Experimental lattice parameters (**a**, **b**, **c**) considered: DLMANT, DMANTL09
- GROMOS Force-field (FF)
  - United-atoms
  - All-atoms

**Qualitative** agreement with experiments (most stable orientation) but SFE shows **significant differences** for different FFs and crystal structures considered

# Cleaving: Mannitol (surface perpendicular to $b$ axis)



Model	Structure	orientation	Total	Lennard-Jones Component	Coulomb Component
ATB	dm	(100)	178	52	126
ATB	dm	(010)	141	79	62
ATB	dm	(001)	264	2	262
GROMOS	dm	(100)	80	60	20
GROMOS	dm	(010)	70	54	16
GROMOS	dm	(001)	92	69	23
ATB	dm09	(001)	179	41	139
ATB	dm09	(100)	161	35	126
ATB	dm09	(010)	155	50	105
ATB	dm09	(120)	139	36	104
ATB	dm09	(011)	139	36	104
GROMOS	dm09	(001)	92	70	22
GROMOS	dm09	(100)	92	70	21
GROMOS	dm09	(010)	75	57	18
GROMOS	dm09	(120)	69	52	17
GROMOS	dm09	(011)	70	53	17

Results in  $\text{mJ}/\text{m}^2$ , dm=DLMANT, dm09=DMANTL09, error  $\approx 1$   $\text{mJ}/\text{m}^2$  in all cases

# VFL approach to compaction

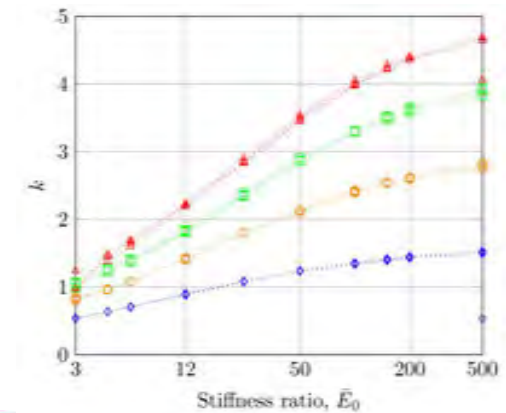
Ben Edmans and Csaba Sinka



# Contact laws for compressible particles

- Contact laws can link particle to bulk behaviour but remain under-developed for compressible particles
- Generic compressible plasticity model proposed
- FE simulations used to investigate influence (right) of material parameters on linear-exponential contact law
- Particle internal zone development mapped (below)

$$\bar{F}_{model}(\bar{\delta}) = \begin{cases} k\bar{\delta}, & \bar{\delta} \leq \bar{\delta}_t \\ k\bar{\delta}_t \exp(a(\bar{\delta} - \bar{\delta}_t)), & \bar{\delta}_t < \bar{\delta} \leq \bar{\delta}_{max} \end{cases}$$



Edmans B.D. and Sinka I.C. 2019. Numerical derivation of a normal contact law for compressible plastic particles. *Mechanics of Materials*. <https://doi.org/10.1016/j.mechmat.2019.103297>

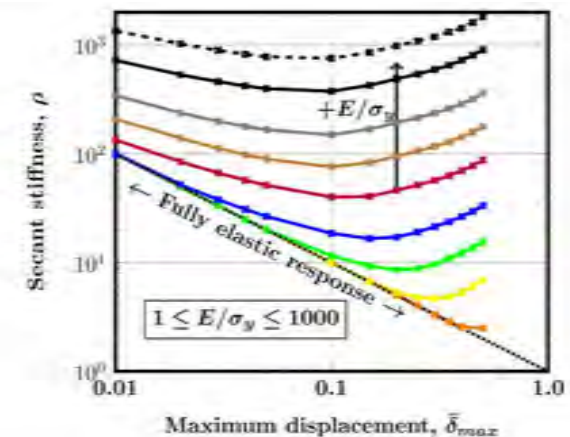
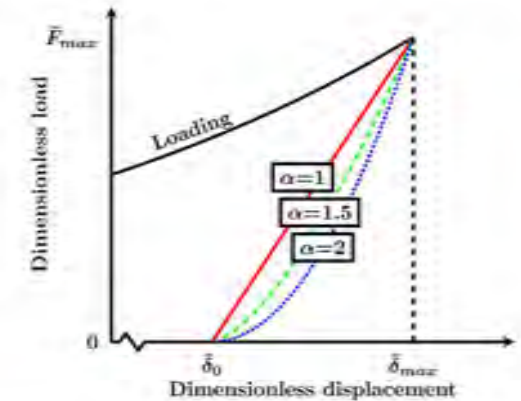


# Particle unloading response

- Accurately representing unloading response is important for DEM at high deformations.
- Stiffness ( $\rho$ ) and nonlinearity ( $\alpha$ ) of unloading load-displacement curves at large displacements investigated
- 560 FE simulations (binary contacts, elastic perfectly-plastic material model) established dependence of  $\alpha$  and  $\rho$  on displacement and material parameters

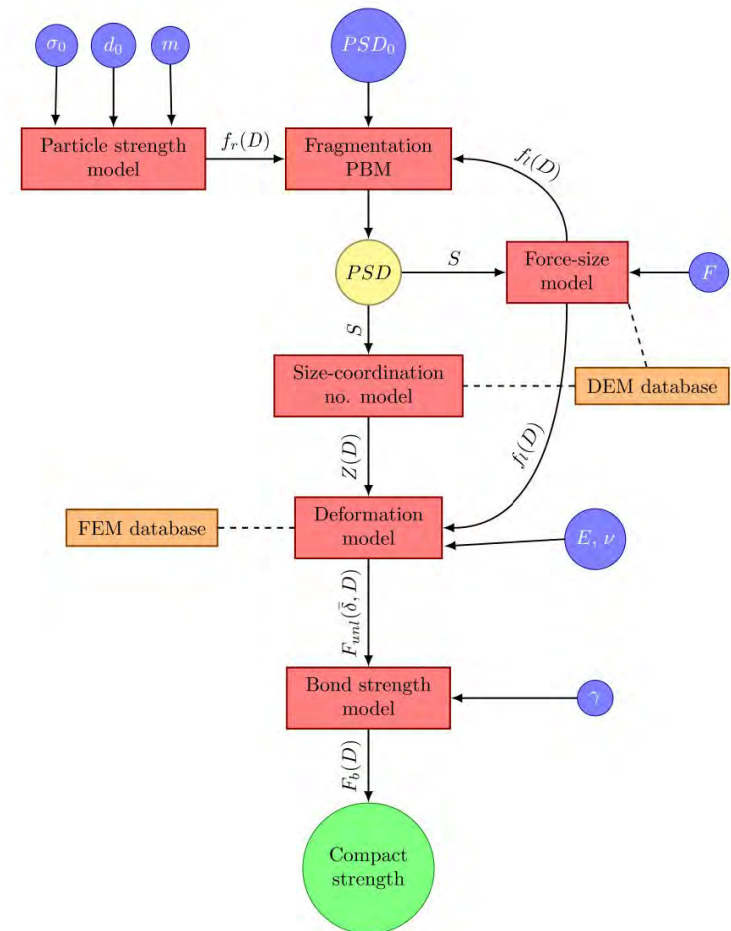
$$\rho(\bar{E}, \nu, \bar{\delta}_{max}) \approx \frac{1}{\bar{\delta}_{max}} + \phi \bar{E} (\gamma_1 \bar{\delta}_{max} + \gamma_2 \bar{\delta}_{max}^{-\gamma_3} + \gamma_4 \nu)$$

Edmans B.D. and Sinka I.C. Unloading of elastoplastic spheres from large deformations. *Powder Technology*. Accepted for publication



# Compact strength prediction

- Goal: predicting strength of compacts from particle/surface properties
- Three main components
  - Fragmentation Population Balance Model
  - FE deformation database for interpolation
  - Adhesion model
- Effective adhesion force function found by calibration
- Key features
  - Modular
  - Represents key compaction mechanisms
  - Component models well supported



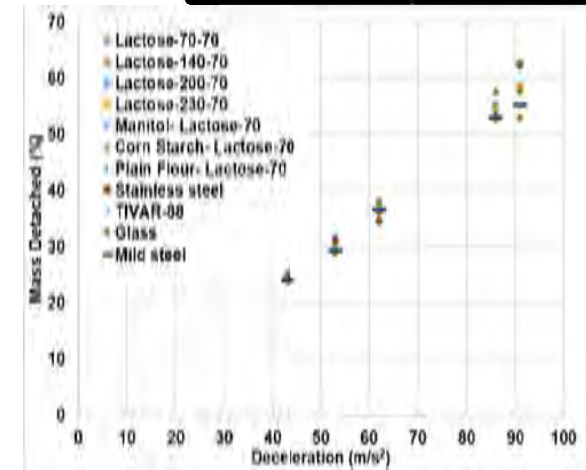
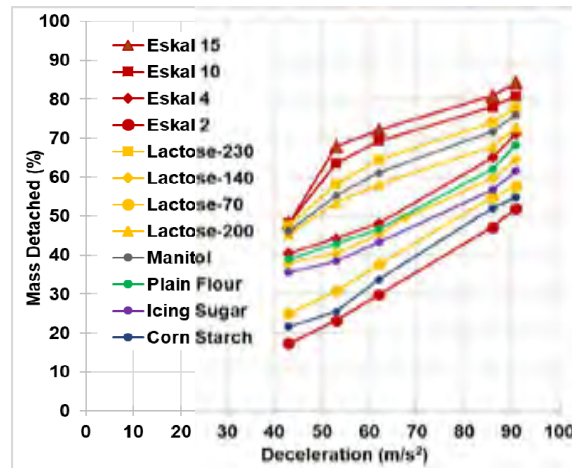
# VFL approach to powder flow

Hamid Salehi, Mike Bradley and Vivek Garg



# 1. Flow in Quasi-static Conditions

- A new technique developed/modified to determine the inter-particle forces of the cohesive powders using a few particles.
- From a few grams at an early stage of formulation, a user can predict whether a bulk of this material will be easy or hard to process.
- An empirical model developed for predicting the flow function from Bond Number/ Adhesion forces.



# 2. Plastic Flow Caking

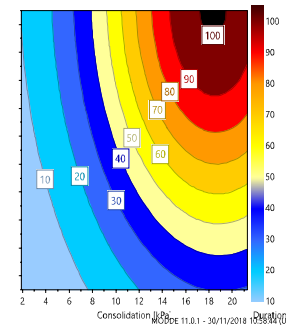
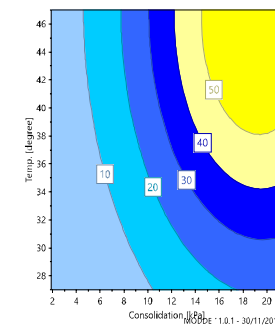
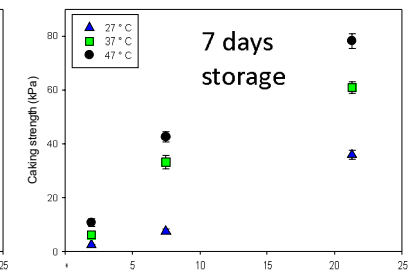
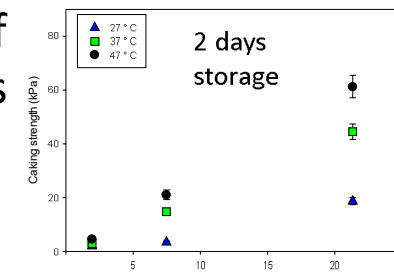
Aim: measuring cake strengths driven by plastic flow mechanisms in storage.

This outperformed the conventional uniaxial unconfined failure caking tester due to the defined location of the failure plane to maximise repeatability, the necessity for a lower quantity of powder, maximised exposed surface and lower wall friction as well as production costs.



A statistical model has been successfully developed to study the effect of each variable on the cake strength.

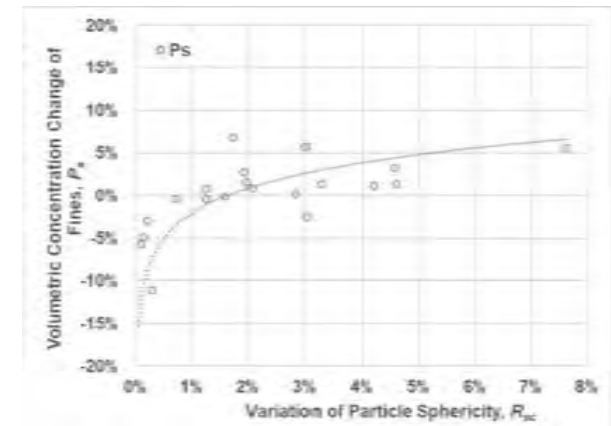
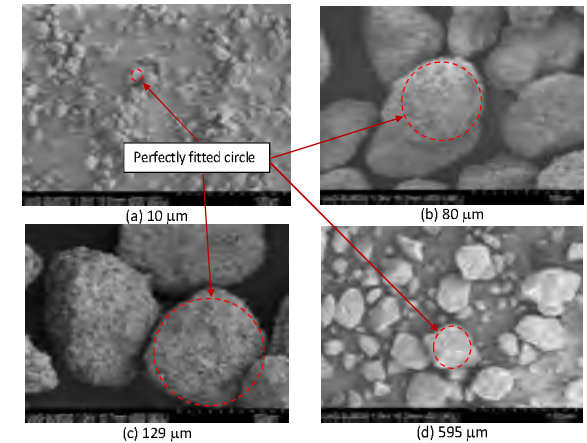
*Salehi et al. Development and application of a novel cake strength tester, Doi: 10.1016/j.powtec.2019.03.024*



# 3. Segregation

Predicting materials propensity to free surface segregation when discharged to form a heap.

- Measure degree of segregation (from top to bottom of slope) by using a scale from perfectly blended (20) to segregated sample (100) based bulk cohesion and particle sphericity.



# VFL approach to powder flow

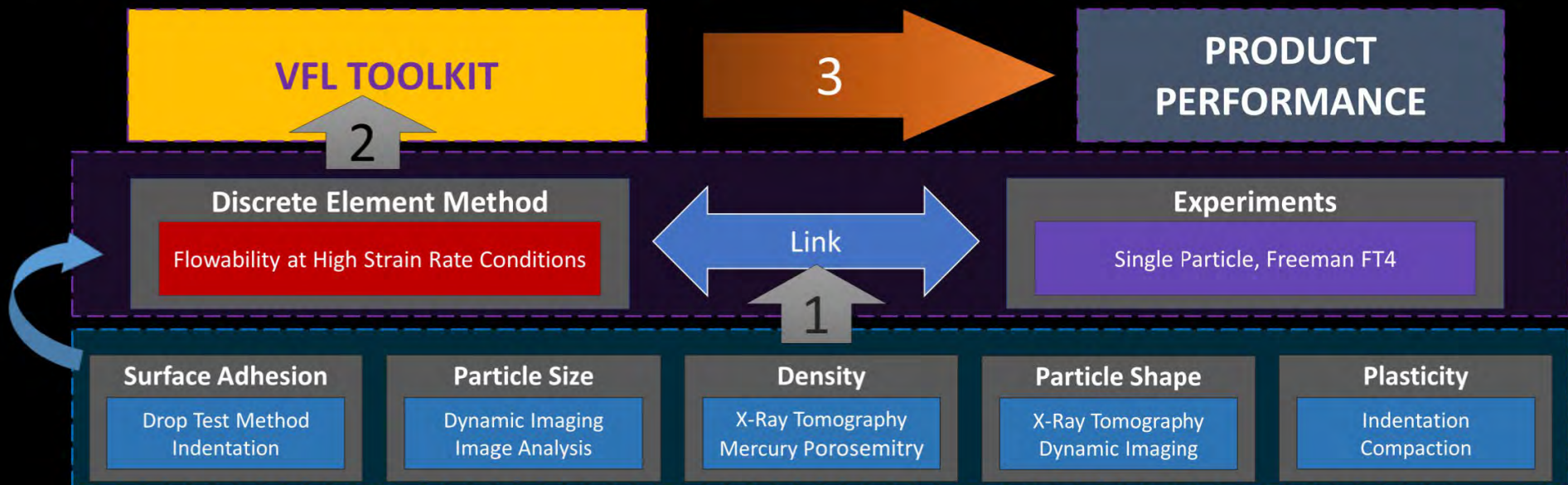
Mehrdad Pasha, Xiaodong Jia and Mojtaba Ghadiri



# Our Approach

## Objectives:

- ❑ Looking at flowability of powder mixtures at high-strain rate.
- ❑ Establish a methodology for calculating properties of powder mixtures using components single particle properties
- ❑ Prediction of rheology of formulated powder mixtures using their flow properties





# Powder Mixture Bond Number

**Bond Number** is the ratio between the force of adhesion and gravitation force:

*'The larger the value of Bond Number, the more cohesive the powder is.'*



Since powder mixtures consist of several components having different values of granular Bond Number, an averaged value must be calculated.

**Mixture Bond Number** can be calculated by averaging the bond number of individual components and introducing a weighting factor (calculated based of fractional surface area of individual components

## Arithmetic Weighted Mean

$$Bo_{mix} = \sum_{i=1}^n \sum_{j=1}^n Bo_{ij} \times w_{ij}$$

## Harmonic Weighted Mean

$$Bo_{mix,har} = \left( \sum_{i=1}^n \sum_{j=1}^n \frac{w_{ij}}{Bo_{ij}} \right)^{-1}$$

## Geometric Weighted Mean

$$Bo_{mix,geo} = \prod_{i=1}^n \prod_{j=1}^n Bo_{ij}^{w_{ij}}$$

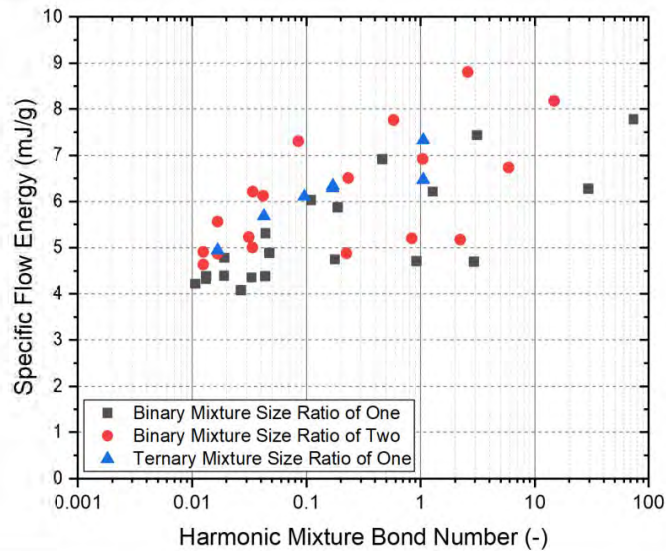
## General Equations

Bond Number	Weighting Factor	Average Weight
$Bo_{g,ij} = \frac{F_{ad,ij}}{W_{ij}}$	$w_{ij} = f_{SA,i} f_{SA,j}$	$W_{ij} = \frac{2W_i W_j}{W_i + W_j}$

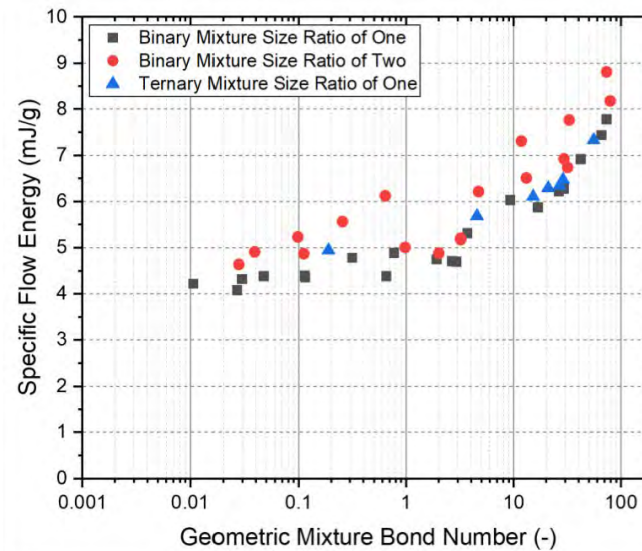
**Note:** in our study, we are considering individual interactions in the mixture. For example, a binary system has four interactions (AA,AB,BA,BB)

# Powder Mixture Bond Number

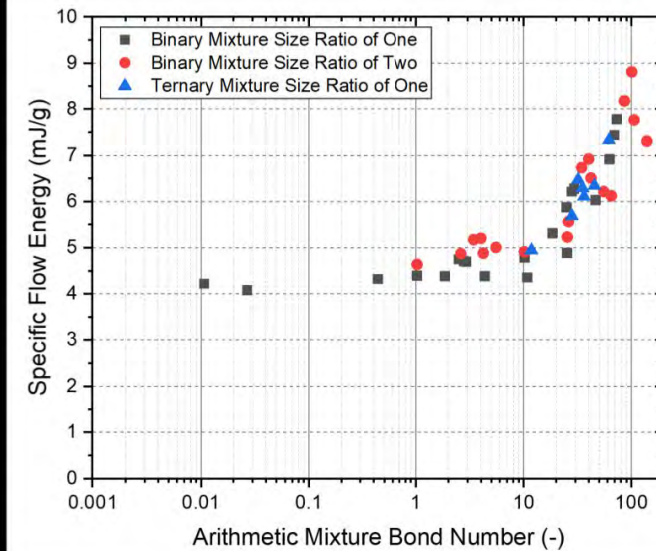
Harmonic Mixture Bond Number



Geometric Mixture Bond Number



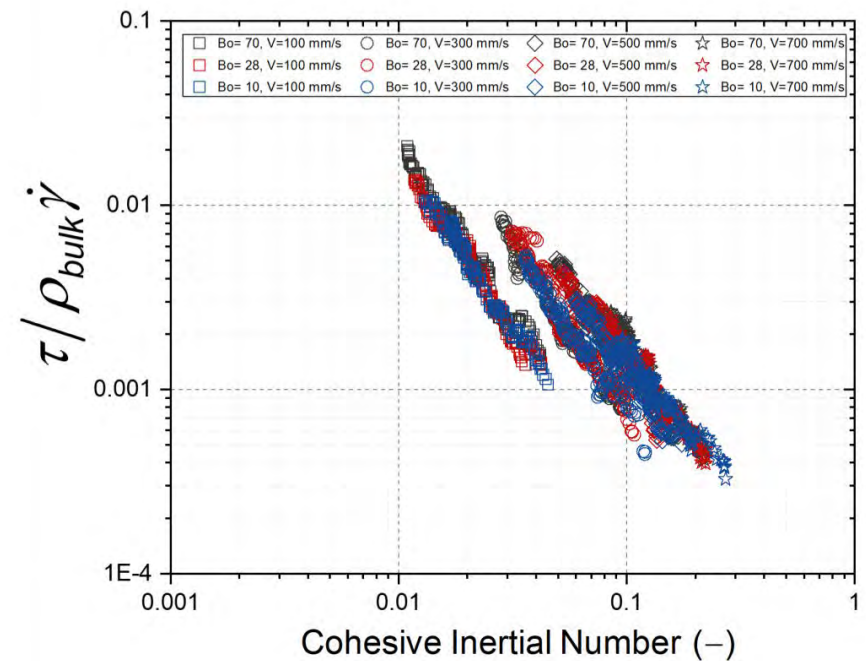
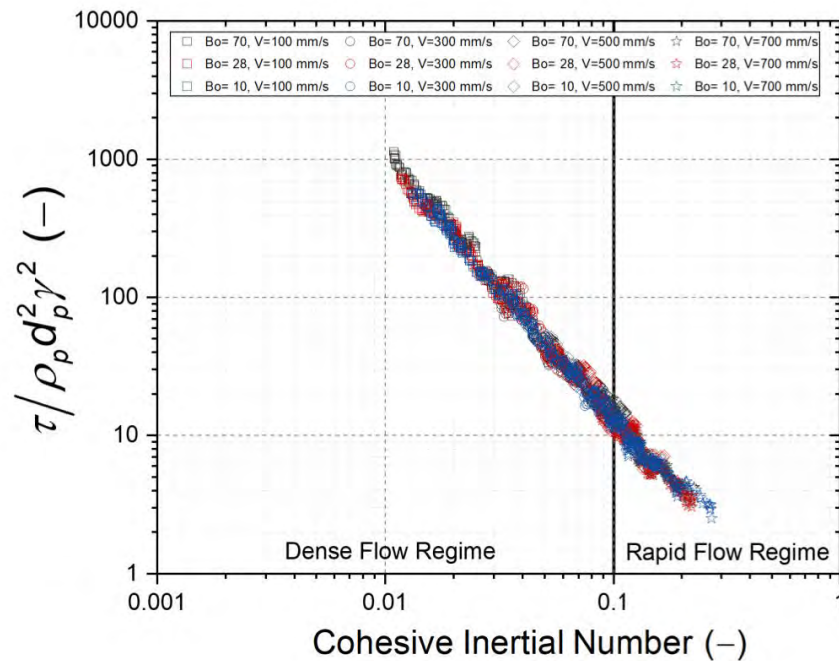
Arithmetic Mixture Bond Number



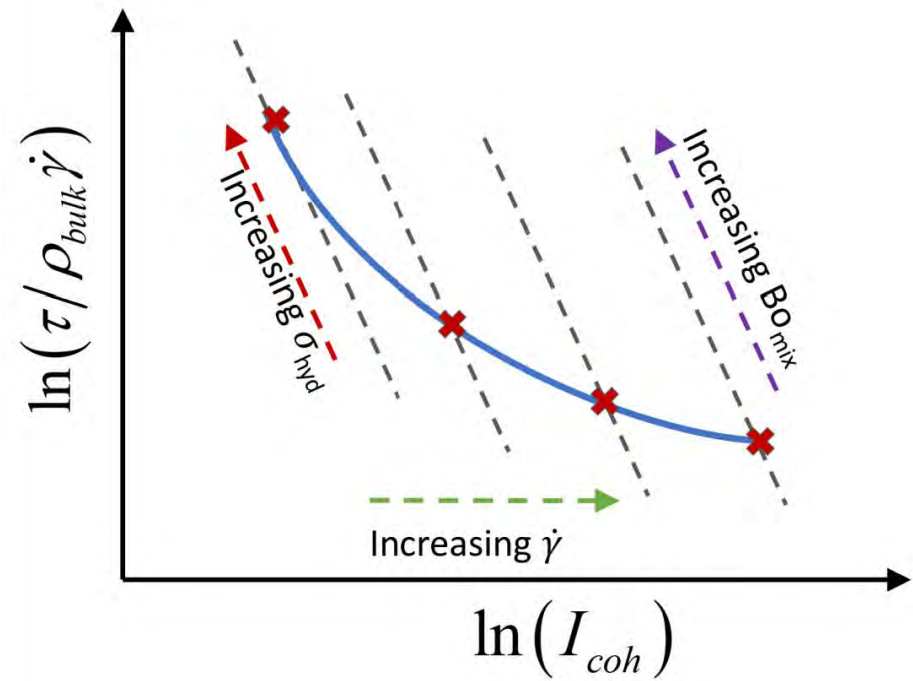
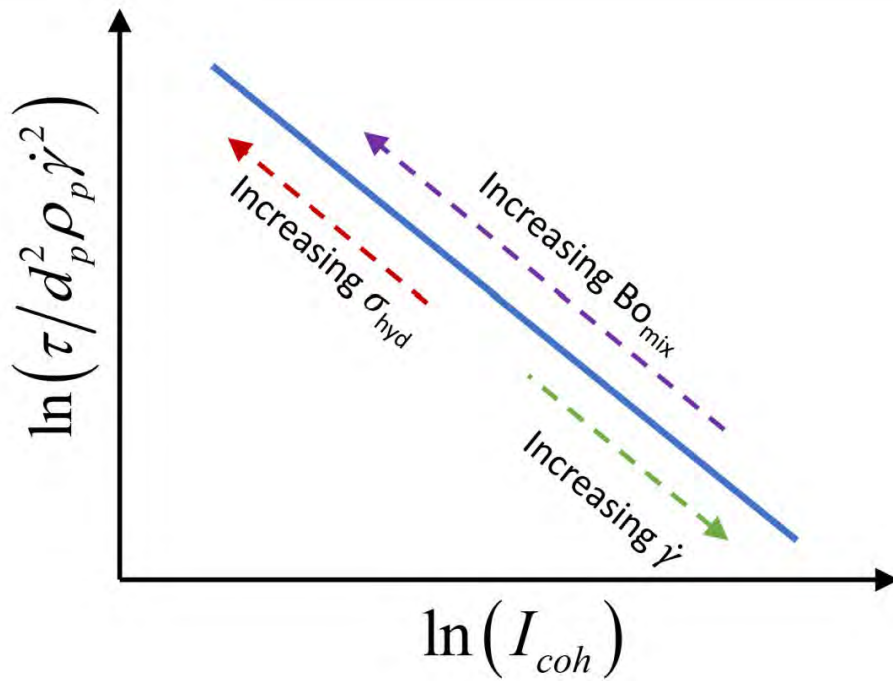
- A clear trend is observed when using geometric and arithmetic bond numbers.
- A good unification of the data can only be achieved with arithmetic mixture bond number
- Specific flow energy only starts rising when  $Bo_{mix,arth} > 10$

Pasha, M., Hekiem, N.L., Jia, X. and Ghadiri, M., 2020. Prediction of flowability of cohesive powder mixtures at high strain rate conditions by discrete element method. *Powder Technology*.

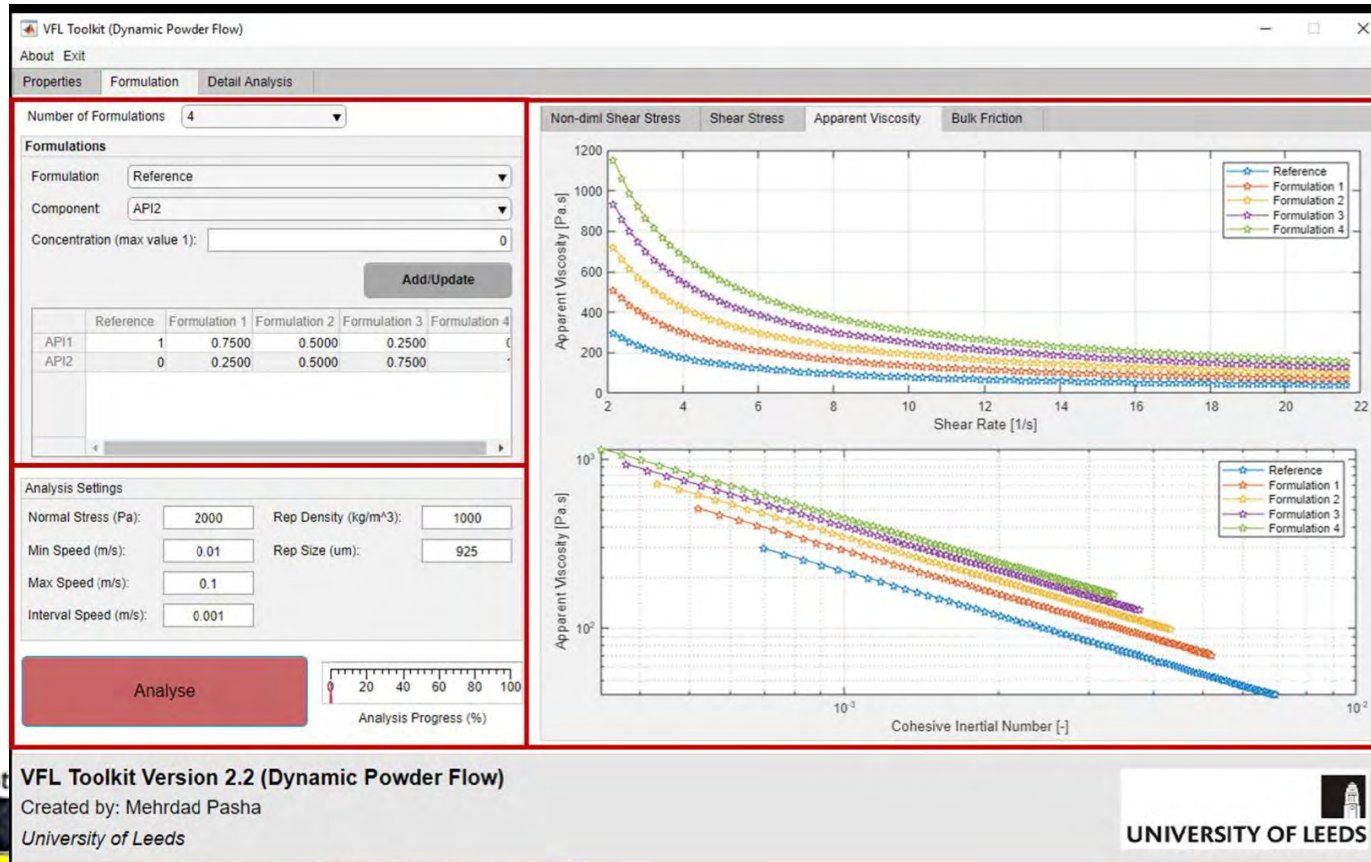
# Rheology of Powder Mixtures



# Rheology of Powder Mixtures



# Rheology of Powder Mixtures



VFL Toolkit Version 2.2 (Dynamic Powder Flow)

Created by: Mehrdad Pasha

University of Leeds



# Concluding remarks

- VFL - a software tool for prediction and optimisation of manufacturability and stability of advanced solids-based formulations
- develops the science base for understanding of surfaces, particulate structures and bulk behaviour to address physical, chemical and mechanical stability during processing and storage
- develops formulation science to link molecule to manufacturability (through experimental characterisation and numerical modelling)
- establishes methodologies to formulate new materials through developing functional relationships considering the limits and uncertainties of these relationships



# Acknowledgement

EPSRC project number EP/N025261/1  
“Virtual Formulation Laboratory  
for prediction and optimisation of  
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of advanced solids based formulations”



## EPSRC

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