

# Influence of Interparticle Forces on Powder Behaviour

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# Interparticle Forces

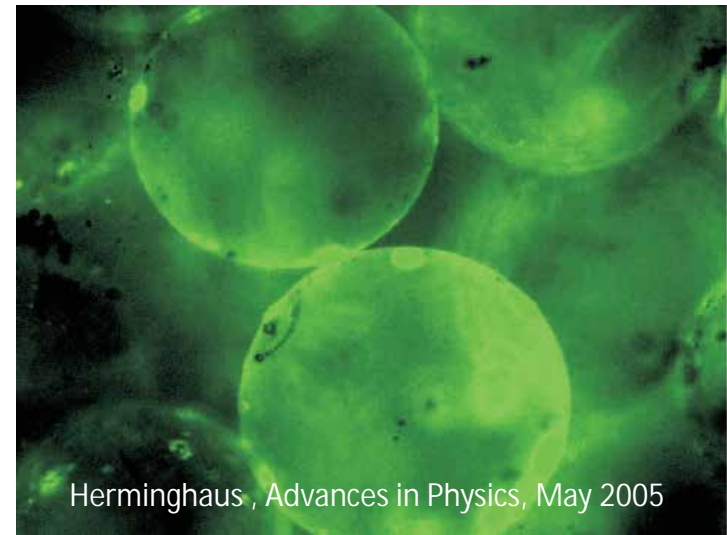
## Capillary Forces

Due the presence of liquid → liquid bridges  
Capillary condensation from a vapour,  
Or by addition of non-volatile liquid.

Static component by Kelvin and Laplace-Young equations

Roughness scale rather than particle size may dictate the capillary forces.

Also a dynamic component important in some cases.



# Interparticle Forces

## Van der Waals Forces

§ Forces arising between molecules

§ Always present

§ Decay as separation squared

Inter-sphere Van der Waals force  $F_{vdw} = \frac{AR}{12a^2}$

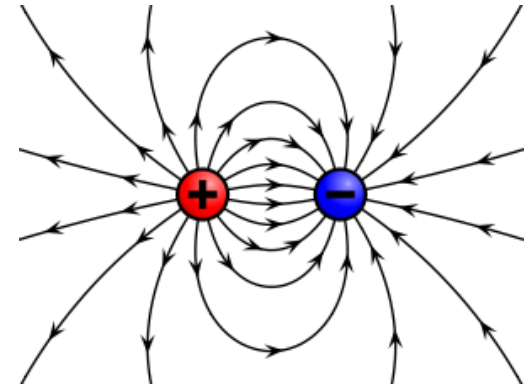
$R$  depends on surface roughness rather than particle diameter

Hamaker constant ,  $A$ , dependent on the material

# Interparticle Forces

## Electrostatic Forces

- § Tribo-electric charging of the particle surface
- § Repulsion between like charges
- § Attraction between opposite charges
- § Both can change powder behaviour



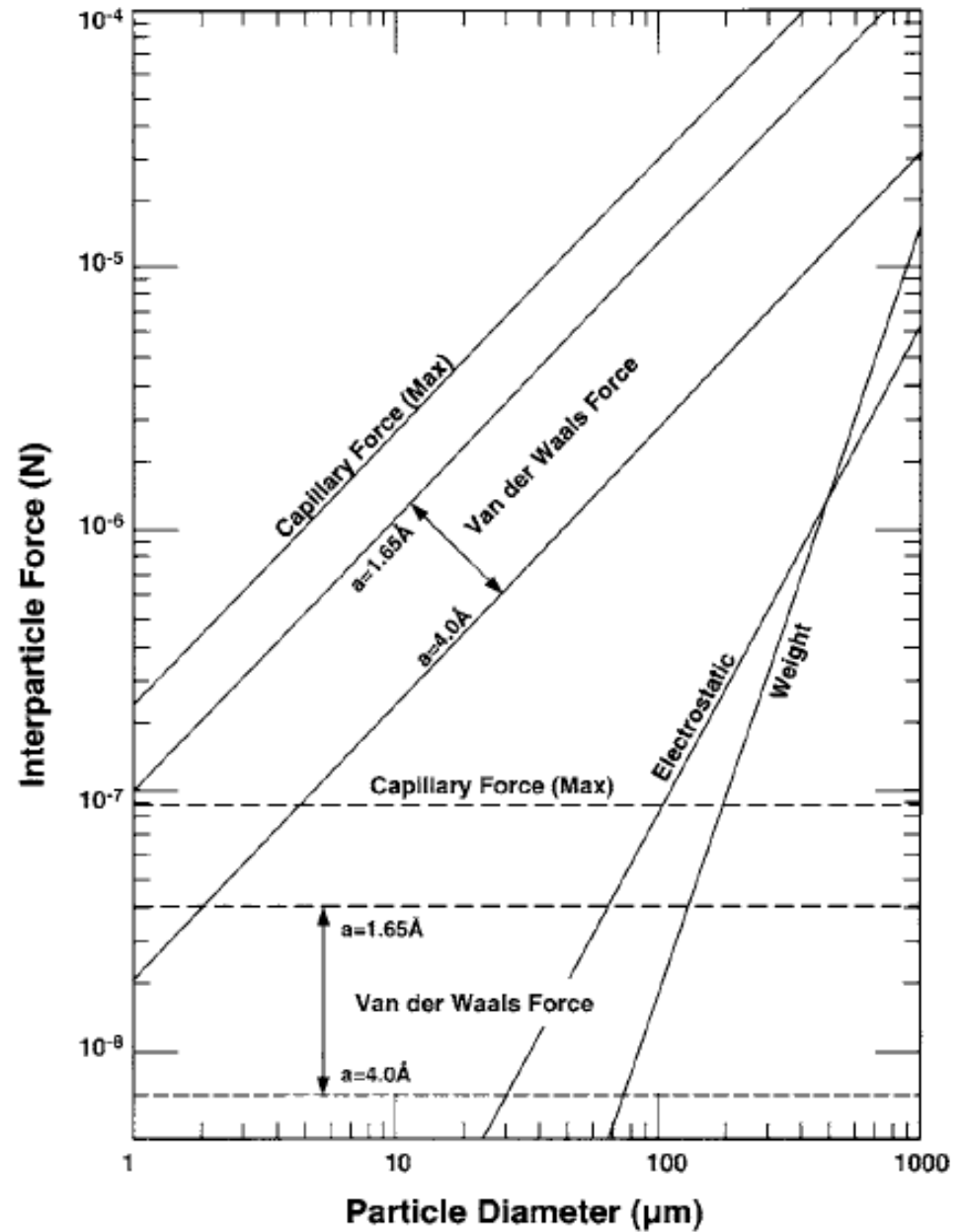
In mixtures of sizes, smaller particles gain opposite charge to larger particles

Important at low humidities with non-conducting particles

$$F_e = k \frac{|q_1||q_2|}{r^2}$$
A diagram showing two point charges: a red circle with a white plus sign (+) on the left and a blue circle with a white minus sign (-) on the right. A dashed line with arrows at both ends connects the centers of the two charges, and is labeled with the letter 'r' below it, representing the distance between them.

# Interparticle Forces

## Relative magnitudes



## **Other forces considered here**

### **Magnetic Forces**

Here concerned with iron or iron containing particles in an externally imposed magnetic field.

Field in different directions. Key features: dipoles, dominant direction, potential for chain formation, cancelling effect occurs

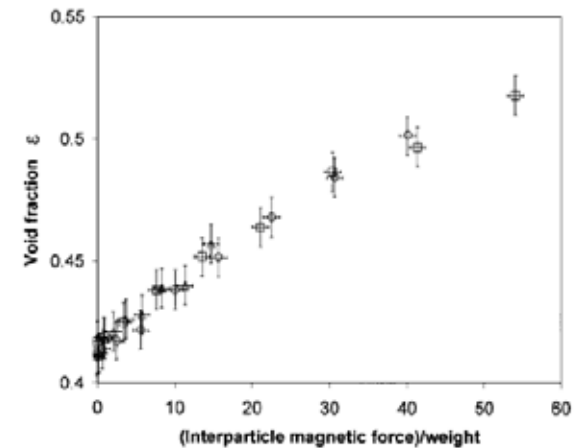
### **Friction Forces**

Note that recent findings show that increase in cohesive force causes increased friction and reduces relative motion of particles.

# Porosity of Randomly Packed Spheres

Forsyth et al, 2001:

- § Experiments with iron particles in a magnetic field
- § Calculation of van der Waals forces



Porosity:

- § Increases with increasing interparticle force (IPF)
- § Governed by IPF/particle wt. (Bond number  $B_o$ )

Yu et al, 2003:

- § Confirmed this result for van der Waals forces and capillary forces
- § Added an empirical expression for porosity:

$$\varepsilon = \varepsilon_0 + (1 - \varepsilon_0) \exp(-mB_o^{-n})$$

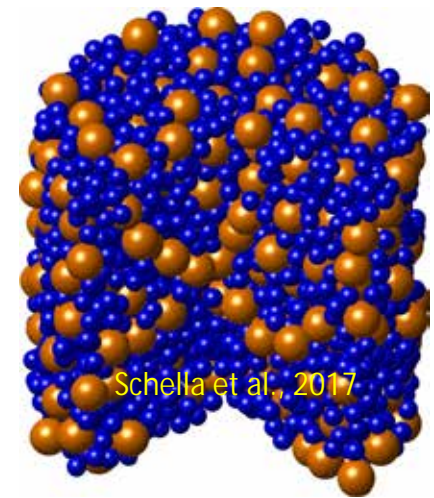
Porosity with zero IPF

# Porosity of Randomly Packed Spheres

**Lumay et al, 2009:**

§ Iron particles in a magnetic field:

§ Confirmed porosity is a function of Bond Number



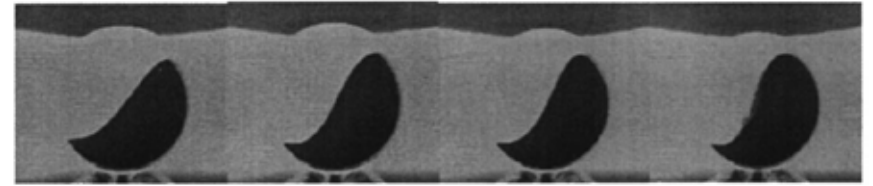
**Schella et al, 2017:**

§ Using controlled electrostatic forces with PTFE spheres:

§ Confirmed the trend of porosity increase with increasing Bond No.



## Angle of Repose



**Forsyth et al, 2001:**

Rotating drum with iron spheres in a variable magnetic field

Showed **static and dynamic** angle of repose (AOR) increase linearly with  $B_0$

**Lumay and Vandewalle, 2010:**

Confirmed AOR results by experiments (magnetised particles)

**Fazekas et al. 2005:**

Confirmed AOR results by simulation of magnetised particles

**Taylor et al. 2008:**

Explained why, for magnetic systems, this effect is much less than as expected (magnetic cancelling effect)

# Angle of Repose – Flow Behaviour

**Forsyth et al, 2002:**

Using two systems:

§ glass spheres in humidity-controlled air

§ iron spheres within a magnetic field

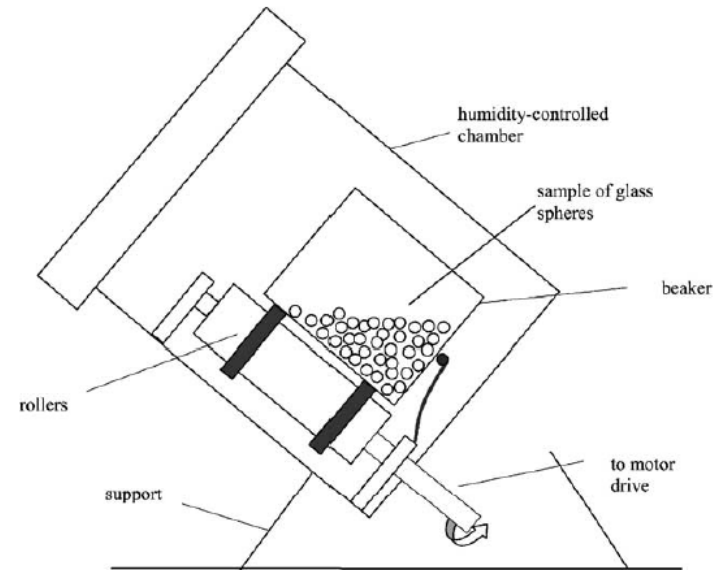
showed that the transition from free-flowing to stick–slip behaviour occurs at a critical ratio of IPF/particle weight ( $Bo$ )

AFM measurements showed force increased monotonically.

**Xiang-Yun Lu et al., 2017:**

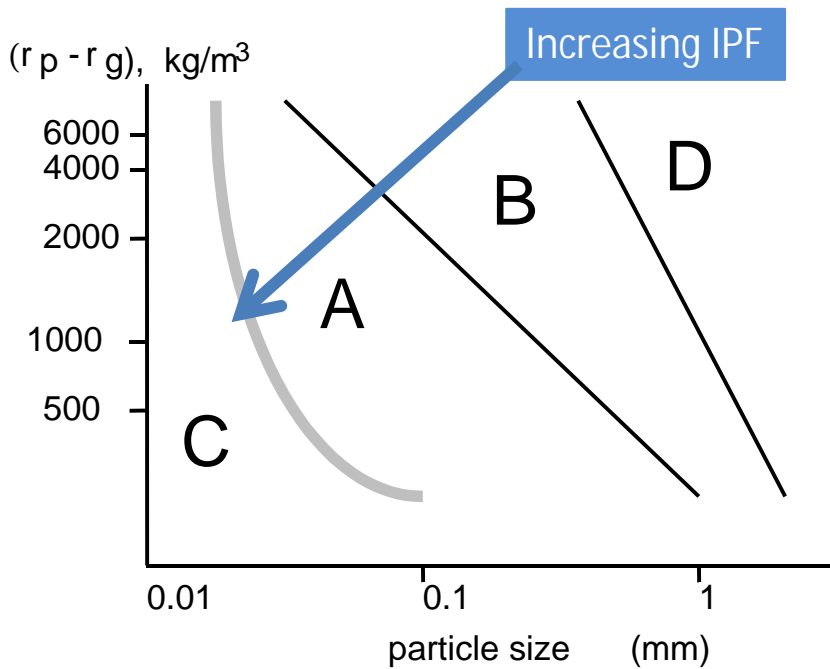
Dry powder inhaler study:

Optimal relative humidity for promoting powder flow and dispersion dependent on the balance between the electrostatic force and the capillary force.



# Fluidization

General trend:

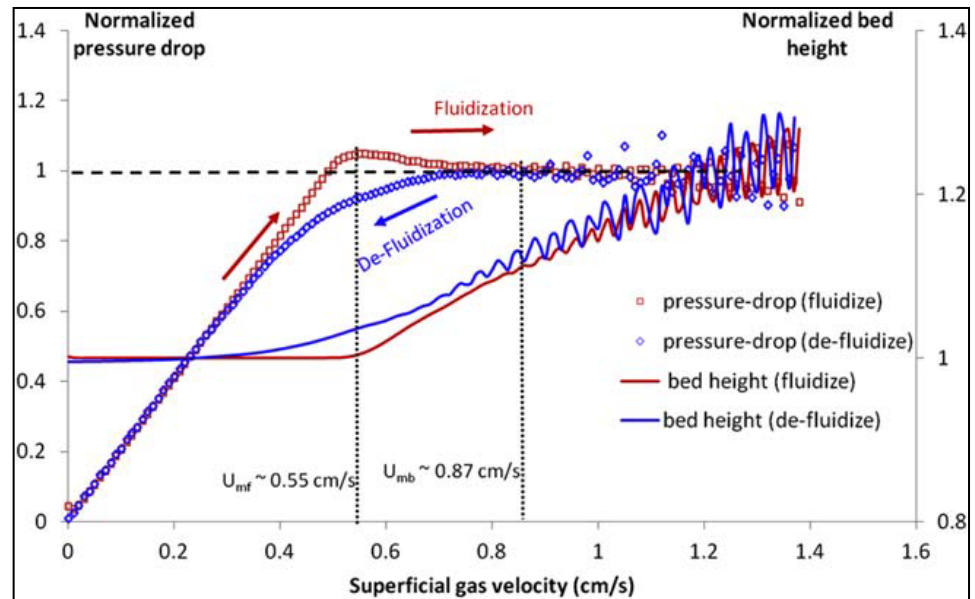


Geldart's classification of powders

B: Bubbling only

A: Non-bubbling range ( $U_{mf}$  to  $U_{mb}$ )

C: Channelling,  $\Delta P < \text{buoyant weight}$



Evidenced by capillary forces, magnetic forces, van der Waals forces

# Fluidization

## Molerus, 1982:

Suggested ratio of IPF/wt determines the BA and AC boundaries in Geldart's classification:

This result supported by many others, but values at boundaries vary.

Examples:

System	IPF/wt at BA
van der Waals estimation (particle radius)	6
van der Waals estimation (asperity radius)	0.3-0.5
DEM simulation	1.0
Added non-volatile liquid	0.02-0.06
Magnetic	2.5

# Fluidization

## AC Boundary

Values of Bond number vary considerably (0.43 to 47) depending on the system and researchers

### However, main conclusion:

Both BA and AC boundaries seem to be governed by critical Bond number.

### Although:

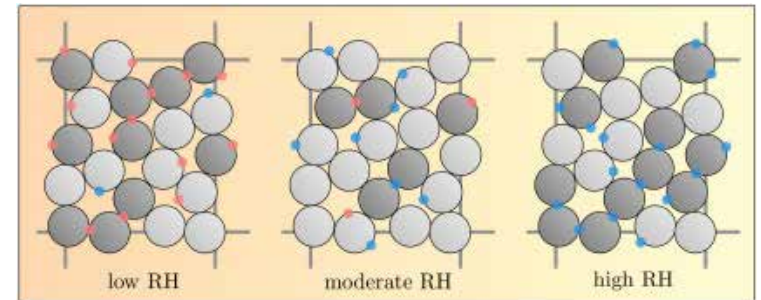
Simulations suggest that A behaviour can occur in the absence of imposed IPF (Pandit et al., Galvin et al., Rhodes et al.)

Support for Foscolo and Gibilaro theory (1984, transition based on hydrodynamics alone)

# Surprising Effect of Interparticle Forces

**Hornbaker et al., Nature, 1997:**

Static angle of repose in **0.8mm** glass beads changes linearly from 25 to 35 degrees with oil layer thickness changing from **5nm to 30nm**



**Vandewalle et al., 2012:**

Packing fraction of **1mm** particles affected by relative humidity (RH).

"A remarkable result ...."

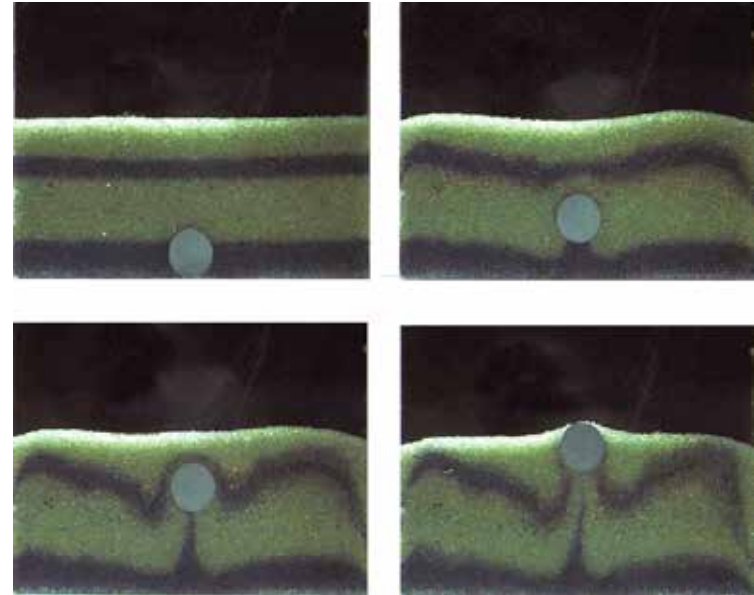
Mobility of particles changes with humidity - low for very low and very high RH  
- highest around 45% RH.

# Surprising Effect of Interparticle Forces

## Yang, 2006, Brazil Nut Effect:

DEM simulation with simplified liquid bridge forces.

Found that small addition of liquid causes large change in rise rate of intruder.



## Rhodes et al, 2003, Brazil Nut Effect:

Order of magnitude change in rise speed of **25mm steel intruder** in a bed of **1mm glass beads** as RH changed.

High RH (capillary condensation) and high electrostatic charge (at low RH) each had the effect of slowing the rise rate. Maximum rise rate at 55% RH.

## Conclusions

Ratio of interparticle force to particle weight ( $Bo$ ) important in factor in determining powder behaviour.

Changes in behaviour often governed by critical values of  $Bo$ .

These critical values of  $Bo$  not associated with step changes in the nature of the forces.

Humidity plays an important and surprising role in influencing behaviour of granular systems:

Low humidity → electrostatic forces

High humidity → capillary forces

Optimum humidity for good flow, dispersion etc: 50-60%

Deserving of much further research